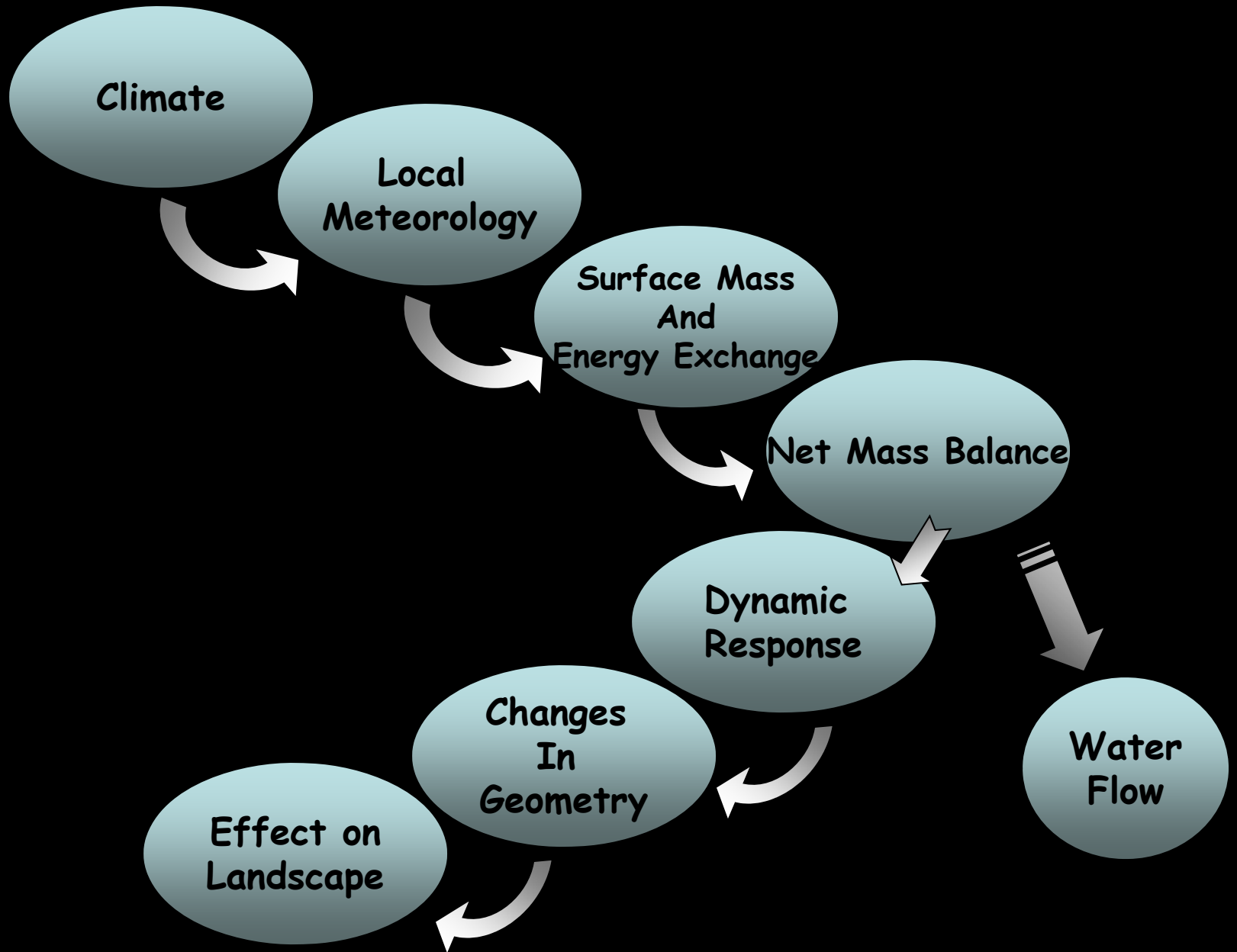
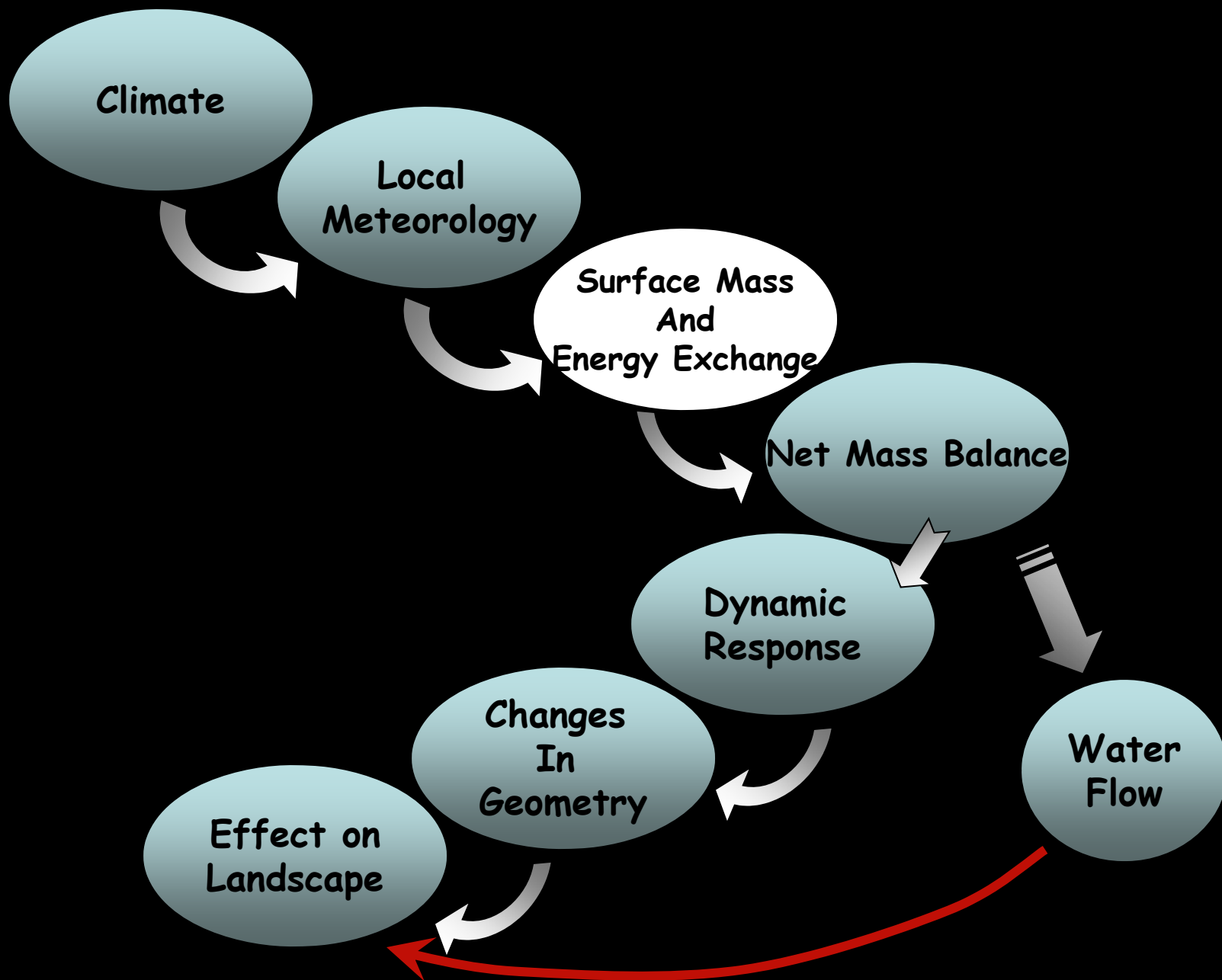
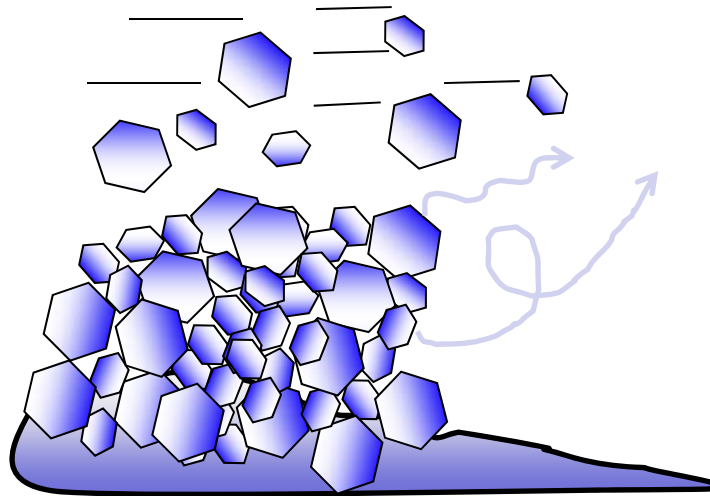
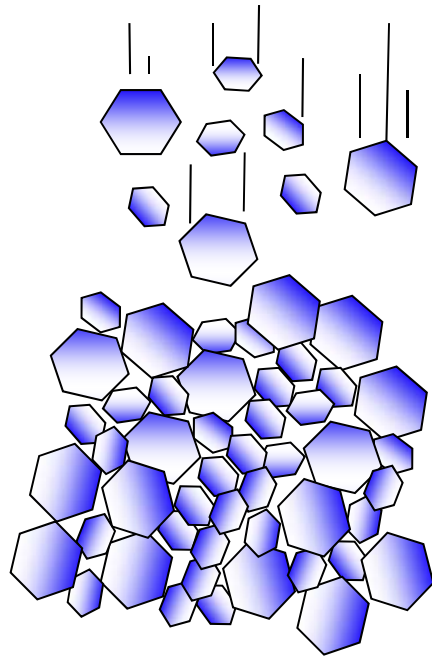


Energy Balance





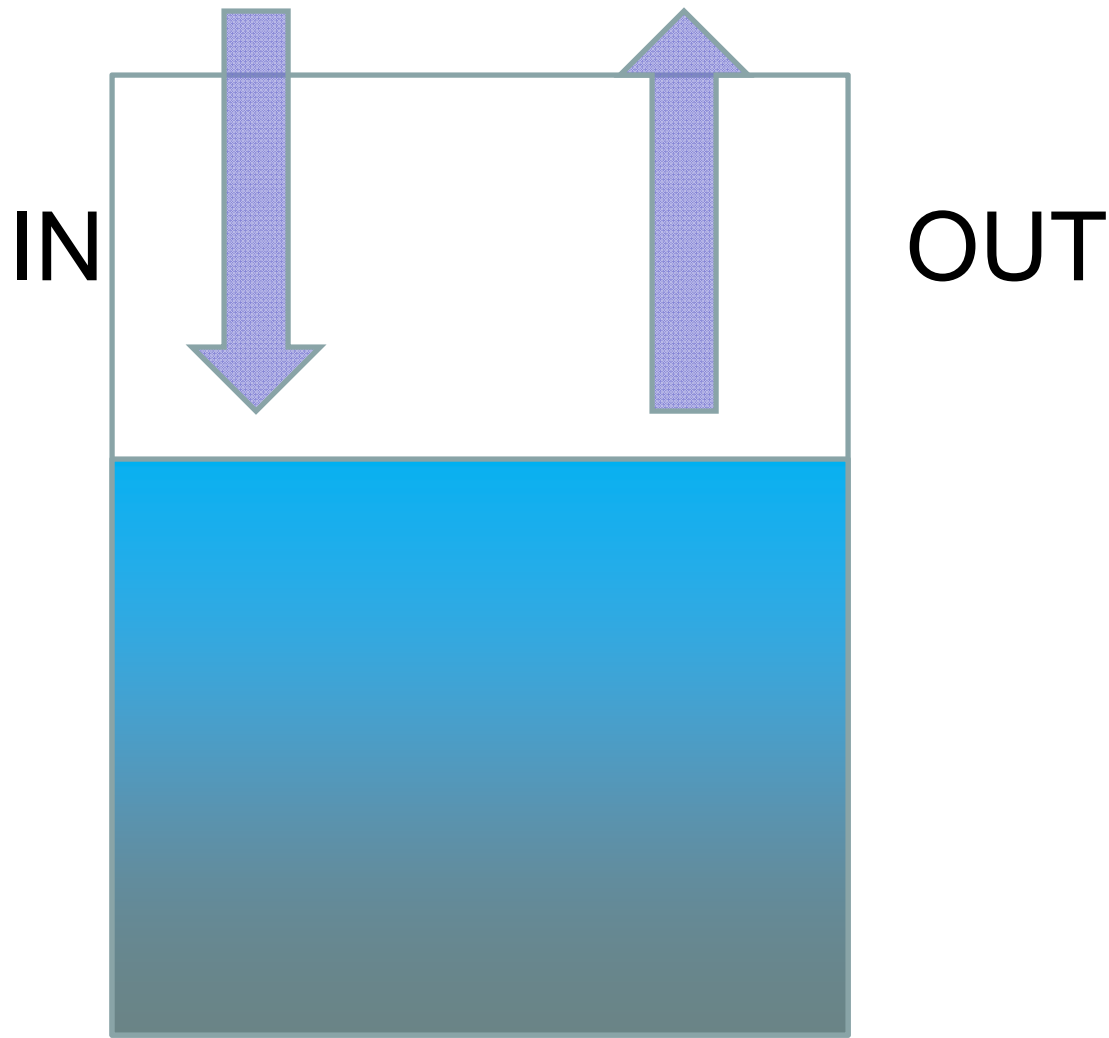
Accumulation - Ablation = Mass Change



Calving
Wind Erosion

Sublimation
Melt

Mass Balance



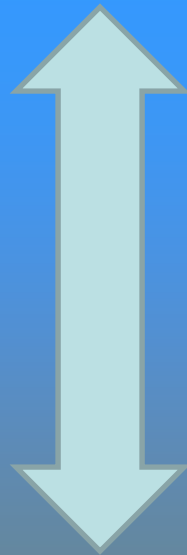
Analogy for heat balance

Surface Energy Balance



Radiation

Turbulent (wind) exchange

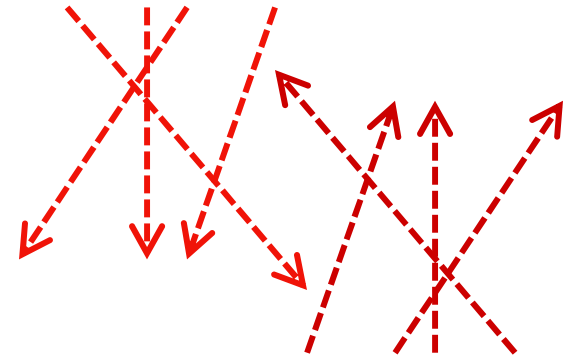


Conduction

Surface Energy Balance



Radiation



Shortwave

Longwave



Surface Energy Balance



Turbulent (wind) exchange

1. Sensible Heat

2. Latent Heat

FLUXES: ATMOSPHERE - GLACIER

$$0 = S\downarrow (1 - \alpha) + L\downarrow - L\uparrow + Q_H + Q_L + Q_m$$

$S\downarrow$	short-wave incoming radiation flux
α	albedo of the surface
$L\downarrow$	long-wave incoming radiation flux
$L\uparrow$	long-wave outgoing radiation flux
Q_H	sensible heat flux
Q_L	latent heat flux
Q_m	phase change

Short Wave Radiation

$S\downarrow (1 - \alpha)$ net shortwave radiation

$S\downarrow$ short-wave incoming radiation flux

α albedo of the surface

Antarctic Snow

$\alpha \sim 0.8$





Clean Ice
 $\alpha \sim 0.5$

A wide-angle photograph of a glacier, likely the Pasterze glacier in Austria. The glacier's surface is highly textured with numerous crevasses and ridges, giving it a rugged, almost rocky appearance. A person in a red jacket and dark pants stands in the middle ground on the glacier, providing a sense of scale. The background shows a valley with snow-dusted mountains under a cloudy sky. The overall color palette is dominated by blues, greys, and whites.

DIRTY ICE

$\alpha \sim 0.2$

Pasterzeglet

Midtalsbreen 2009

Long Wave Radiation

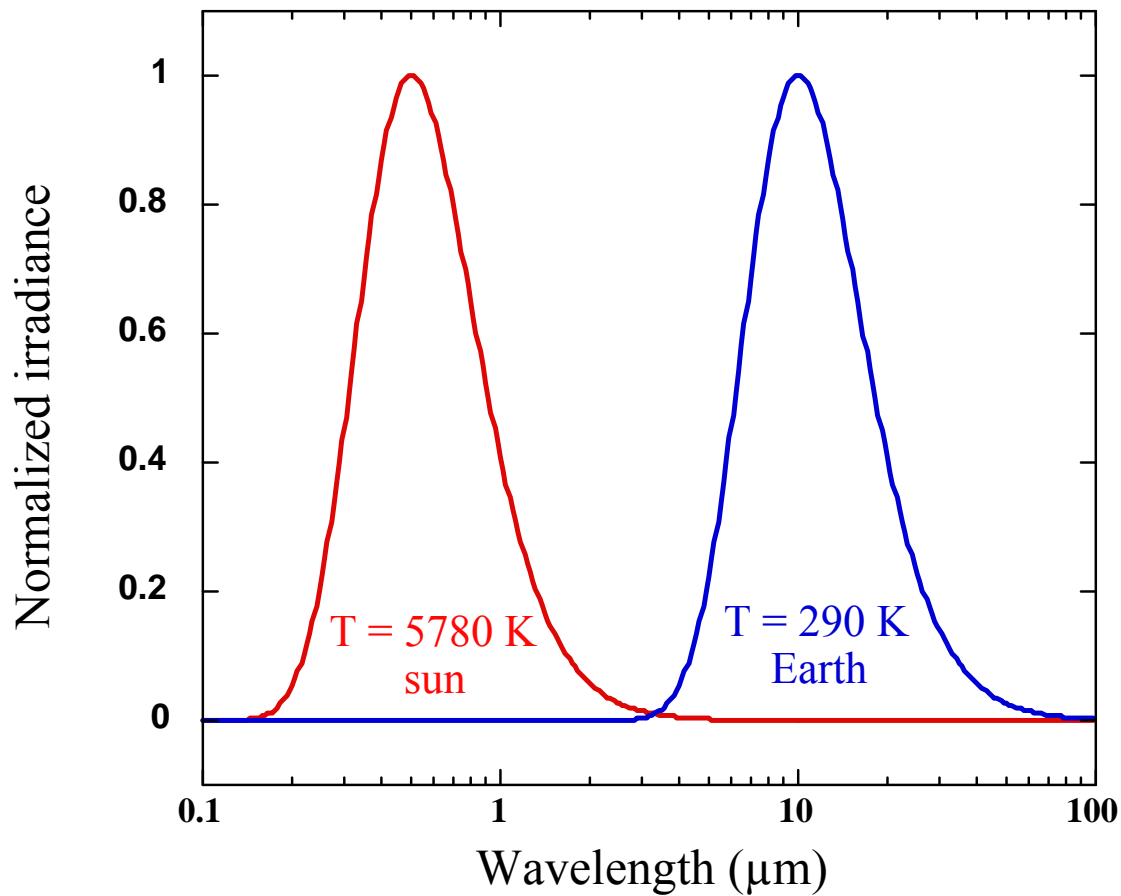
$$L\downarrow - L\uparrow$$

$L\downarrow$ long-wave incoming radiation flux

$L\uparrow$ long-wave outgoing radiation flux

SHORT- AND LONG-WAVE RADIATION

Black body radiation



$$Q = \sigma T^4$$

Q flux (irradiance)

σ Stefan Boltzmann constant

($5.67 \cdot 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$)

T temperature

$$Q = \varepsilon \sigma T^4$$

ε emmissivity

TURBULENT FLUXES

$$Q_H + Q_L$$

Vertical transport of properties of the air by eddies

Turbulence is generated by wind shear (du/dz)

Turbulent fluxes increase with wind speed

Heat: sensible heat flux, Q_H

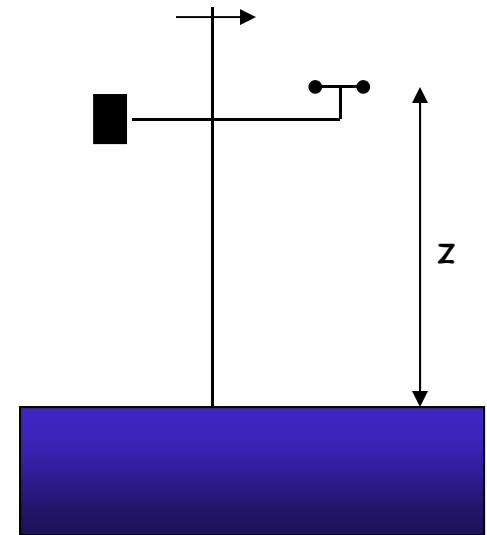
Water vapor: latent heat flux, Q_L

SENSIBLE HEAT FLUX (Q_H)

calculated with the "bulk method"

$$Q_H = \rho_a C_{pa} \frac{\kappa^2 u (T - T_s)}{\left(\ln \frac{z}{z_0} + \frac{\alpha_m z}{L_{ob}} \right) \left(\ln \frac{z}{z_T} + \frac{\alpha_h z}{L_{ob}} \right)}$$

- ρ_a air density
- C_{pa} specific heat capacity of air
- κ von Karman constant
- u wind speed
- T air temperature at height z
- T_s surface temperature
- z_0 momentum roughness length
- z_T roughness length for temperature
- α_m, α_h constants
- L_{ob} Monin-Obukhov length (depends on u and $T - T_s$)



LATENT HEAT FLUX (Q_L)

calculated with the "bulk method"

$$Q_L = \rho_a L_s \frac{\kappa^2 u (q - q_s)}{\left(\ln \frac{z}{z_0} + \frac{\alpha_m z}{L_{ob}} \right) \left(\ln \frac{z}{z_q} + \frac{\alpha_h z}{L_{ob}} \right)}$$

ρ_a	air density
L_s	latent heat of sublimation
k	von Karman constant
u	wind speed
q	specific humidity at height z
q_s	surface specific humidity
z_0	roughness length for velocity
z_q	roughness length for water vapor
α_m, α_h	constants
L_{ob}	Monin-Obukhov length (depends on u and $T - T_s$)

measure short-wave radiation
with a pyranometer (glass
dome)



measure long-wave radiation
with a pyrgeometer (silicon
dome)



INSTRUMENTS

measure sensible heat flux
with a sonic anemometer



Greuell, 2003



ZERO-DEGREE ASSUMPTION

Assumption: surface temperature = 0°C

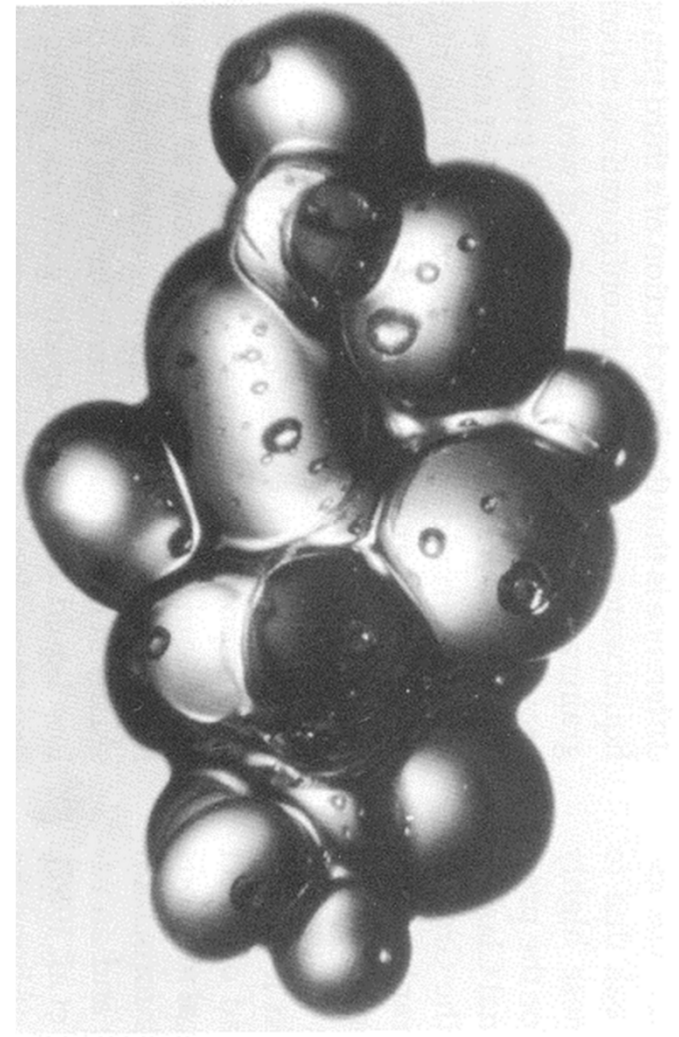
Leads to:

$Q_0 > 0$: Q_0 is consumed in melting

$Q_0 \leq 0$: nothing occurs

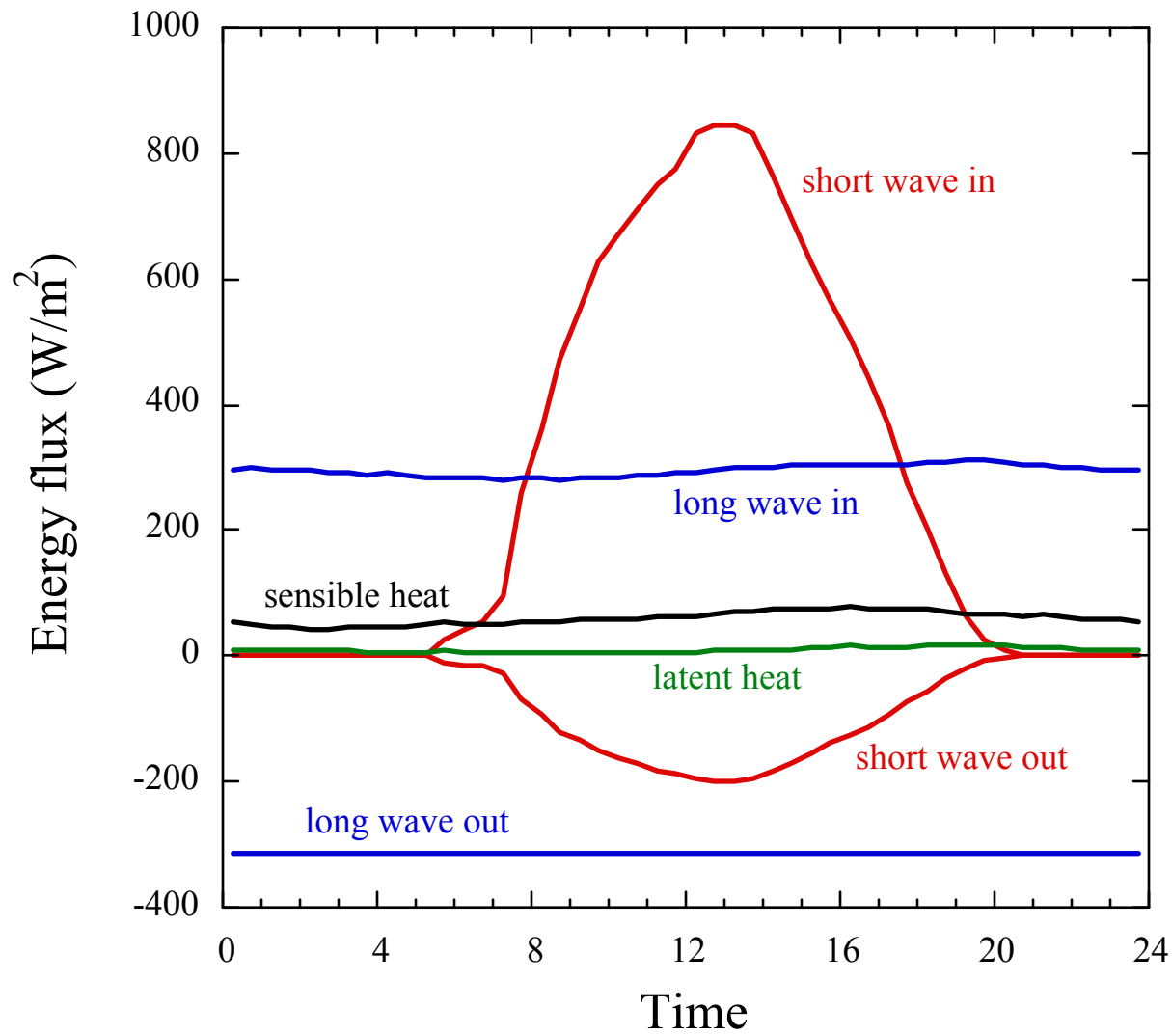
Assumption okay when melting conditions are frequent

Not okay when positive Q_0 causes heating of the snow (spring, early morning, higher elevation)

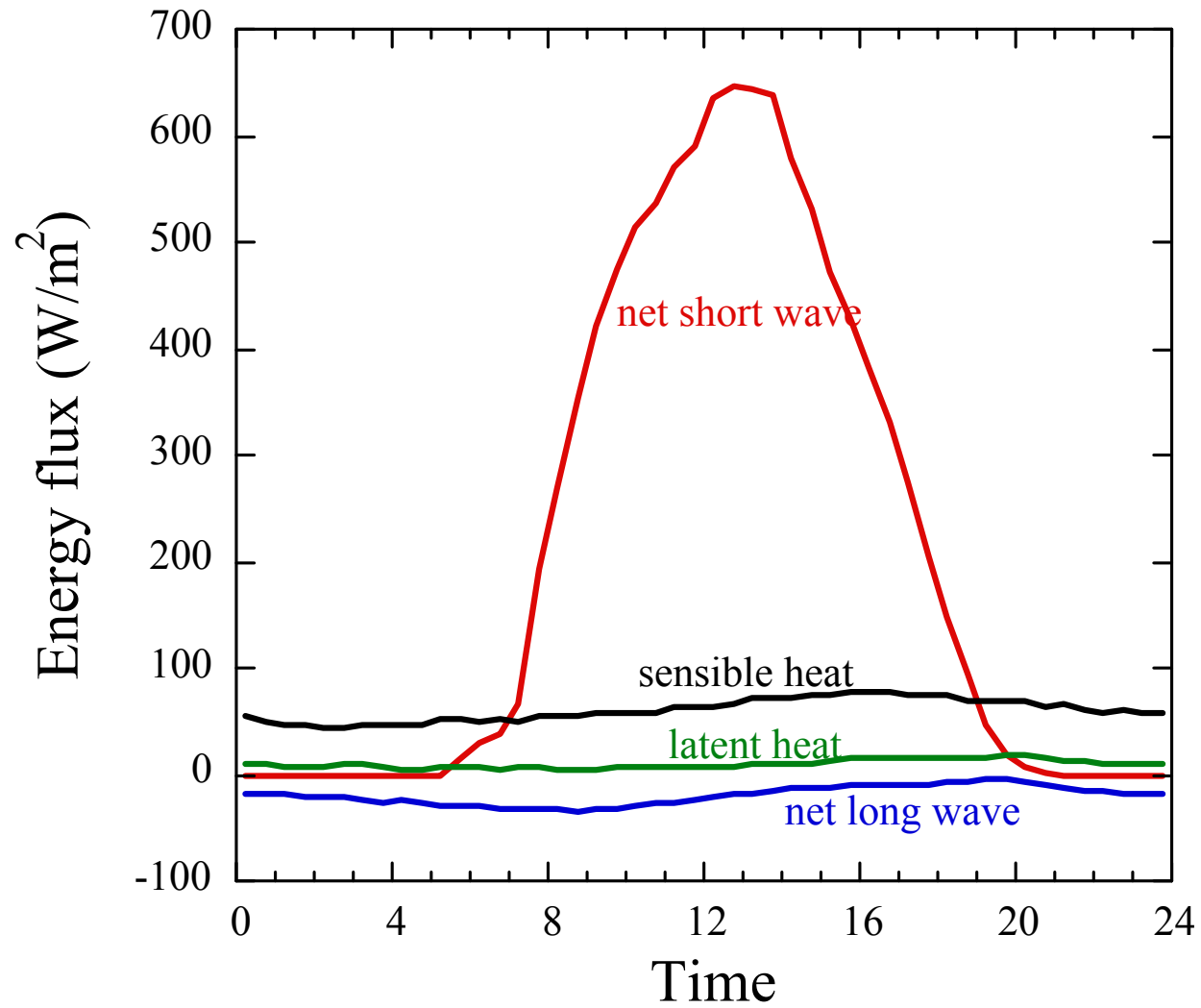


Diurnal Variation

site on glacier ice in summer



NET FLUXES



R = net radiation

S = sensible heat

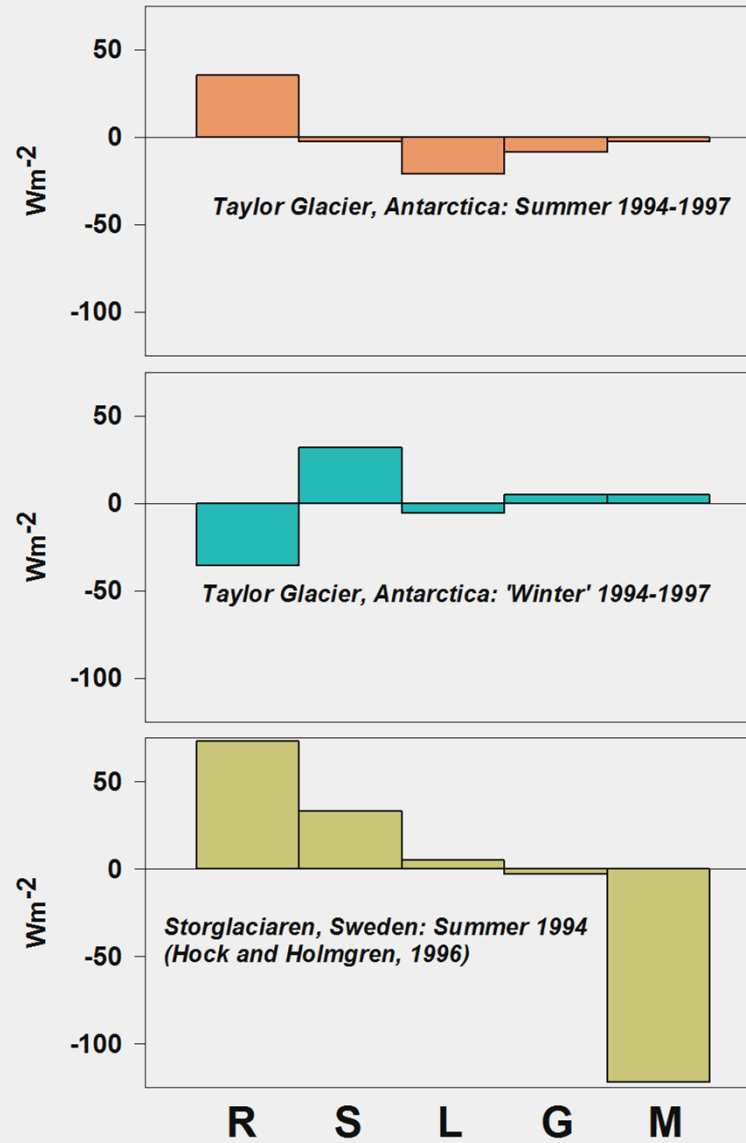
L = latent heat

G = ground heat flux

M = melt

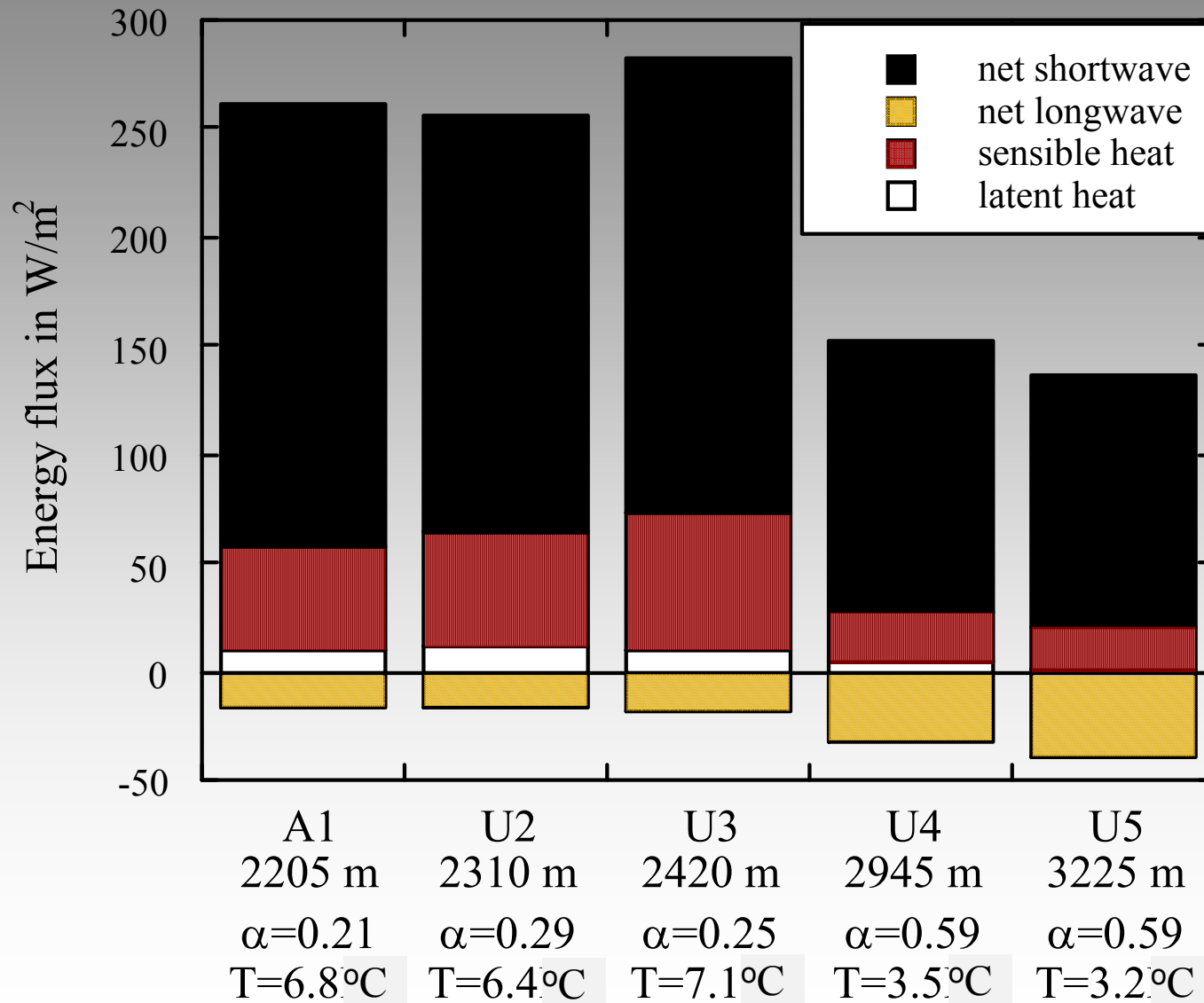
POSTIVE FLUX IS TOWARDS
THE SURFACE

Average Daily Energy Balance Terms

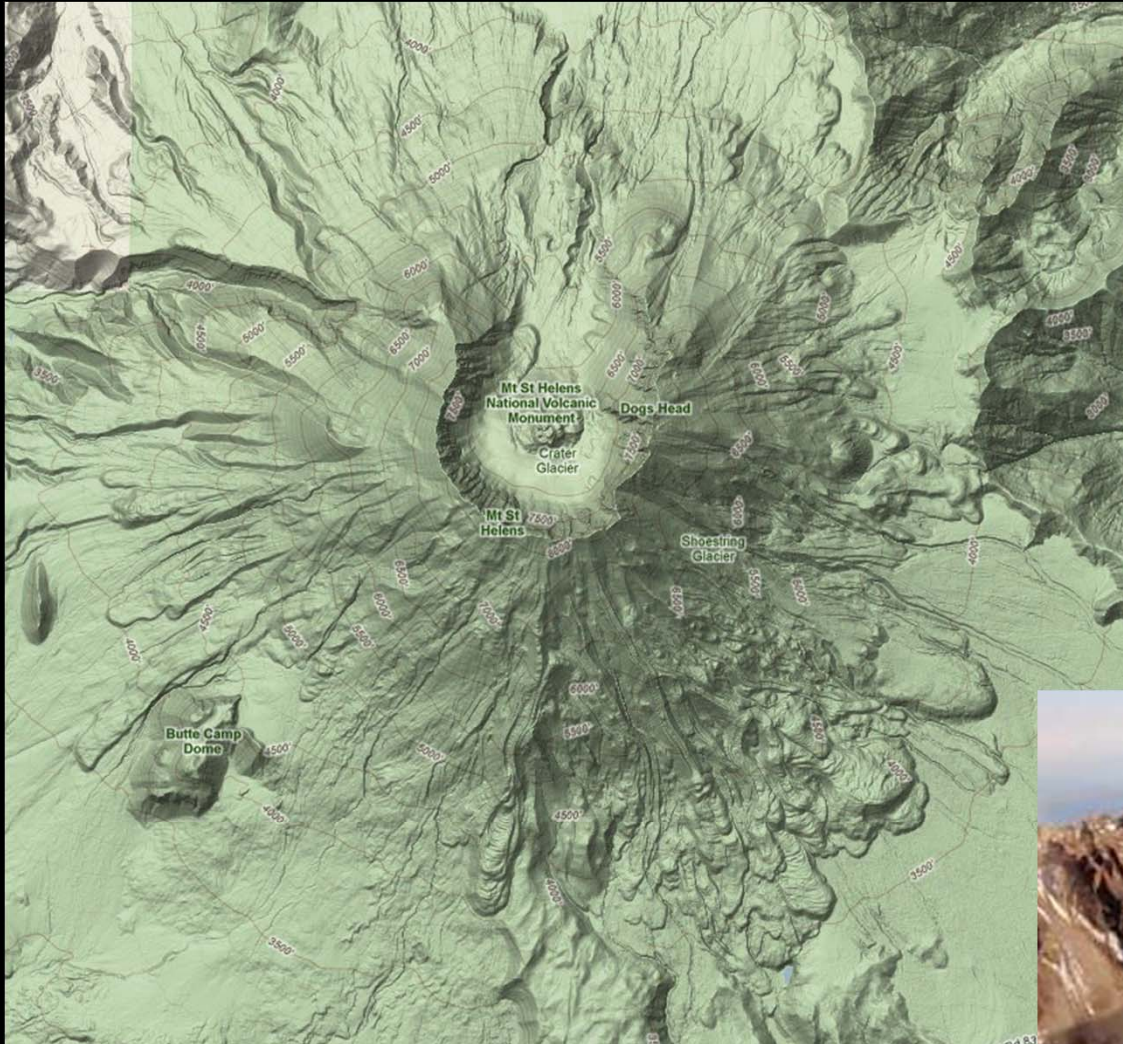


ENERGY BALANCE AT 5 ELEVATIONS

Pasterzegletscher



Effect of Solar Radiation

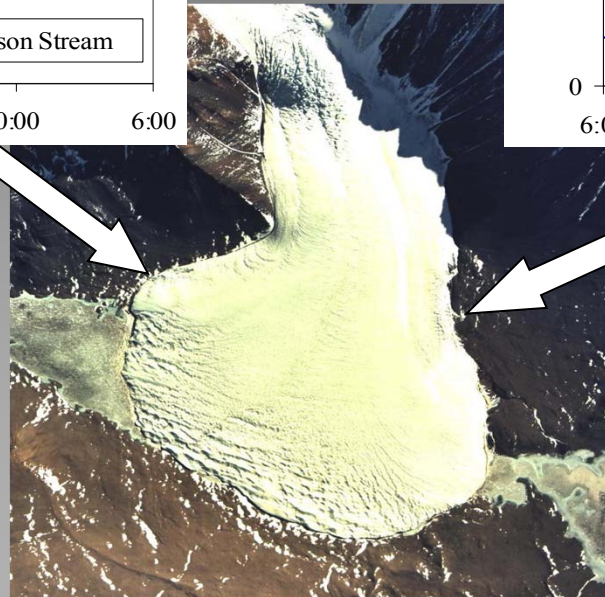
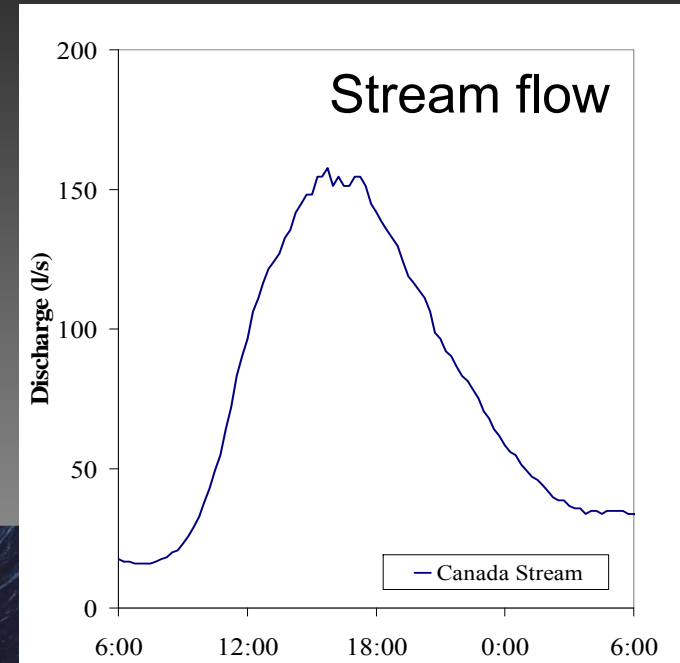
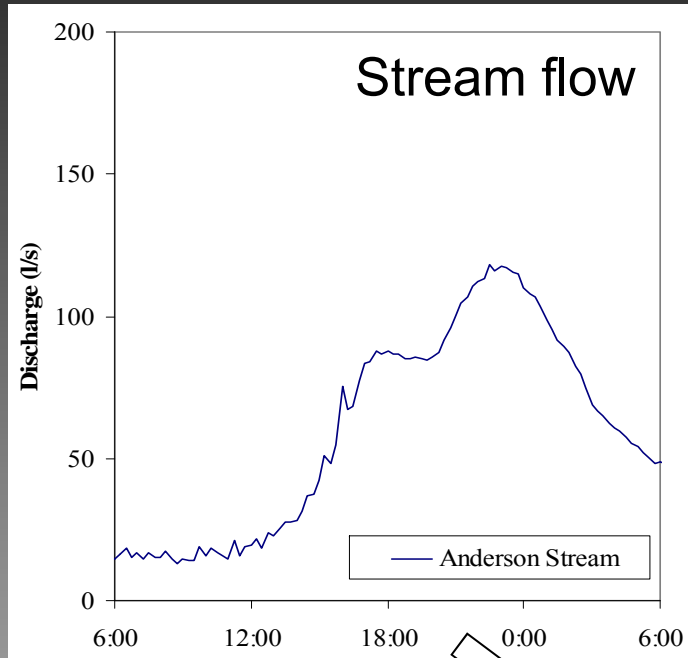


Google Maps



Rueters

Effect of Solar Radiation



Effect of Solar Radiation, Turbulent Exchange

Dec-Jan 1996-1997

Ablation 27.4 cm

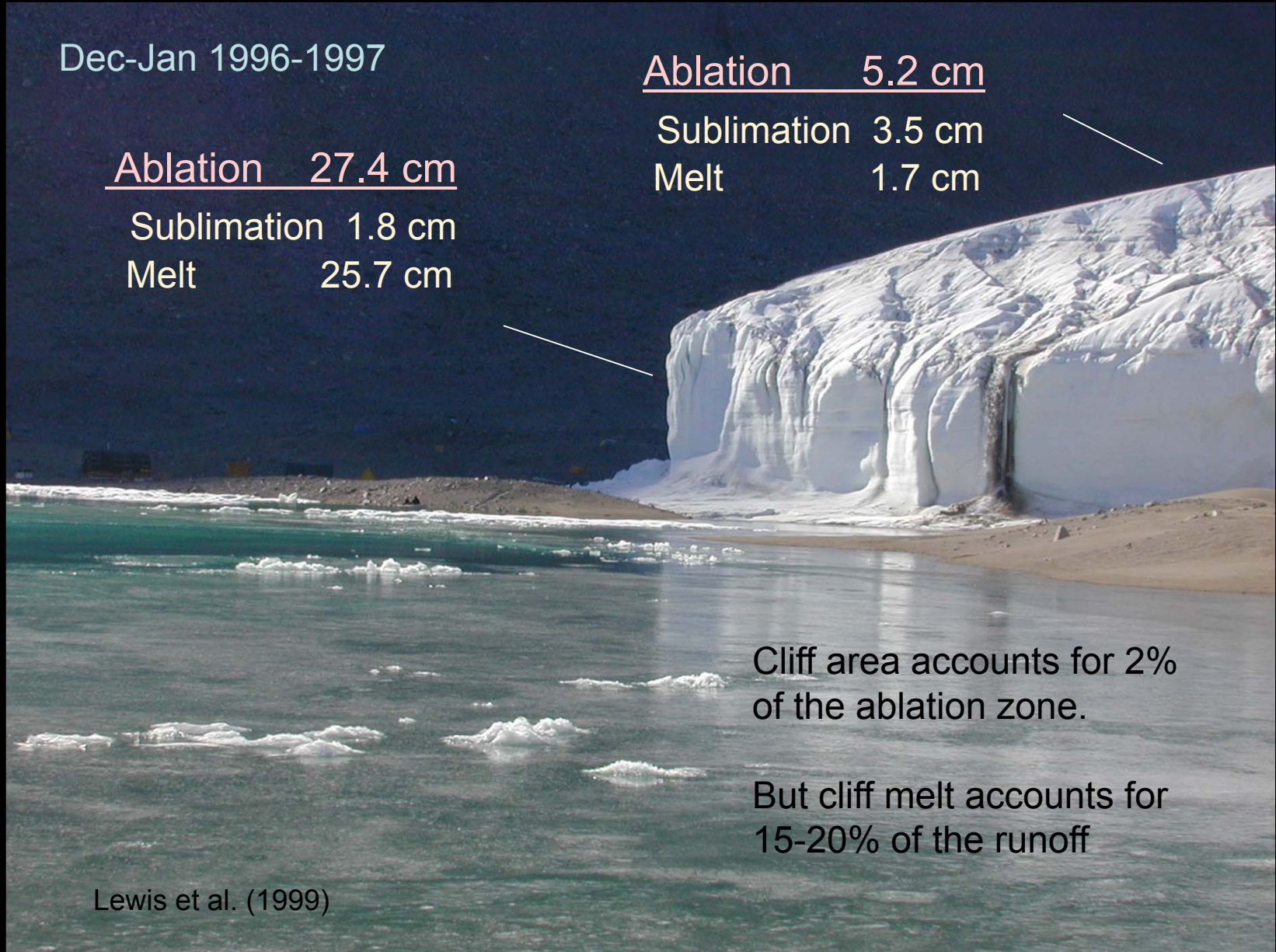
Sublimation 1.8 cm

Melt 25.7 cm

Ablation 5.2 cm

Sublimation 3.5 cm

Melt 1.7 cm



Cliff area accounts for 2% of the ablation zone.

But cliff melt accounts for 15-20% of the runoff

Lewis et al. (1999)

Effect of Solar Radiation, Turbulent Exchange



Penitentes are the name of the caps of the nazarenos; literally those doing penance for their sins. *Photo: Sanbec Wikipedia*



Neve Penitentes Upper Rio Blanco, Argentina *Photo: Arvaki Wikipedia*



Mount Rainier
0.5 m tall.

Photo: Mark Sanderson Wikipedia



Notice the tilt angle

person

DEGREE-DAY METHOD

$$M = \beta T_{\text{pdd}}$$

M: melt

β : degree-day factor [$\text{mm day}^{-1} \text{K}^{-1}$]

T_{pdd} : sum of positive daily mean temperatures

Why does it work:

- net long-wave radiative flux, and sensible and latent heat flux \sim proportional to T
- feedback between mass balance and albedo

Advantages:

- computationally cheap
- input: only temperature needed

Disadvantages:

- more tuning to local conditions needed: e.g. b depends on mean solar zenith angle
- only sensitivity to temperature can be calculated

REGRESSION MODELS

$$M_n = c_0 + c_1 T_s + c_2 P_w$$

M_n : mean specific mass balance

c_i : coefficients determined by regression analysis

T_s : Annual mean summer temperature

P_w : Winter Precipitation



End